

Production of high- p_t particles in AuAu and dAu

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⇒ Motivation. —→ Medium properties.

⇒ Initial state.

↪ nuclear PDF.

↪ Saturation ??

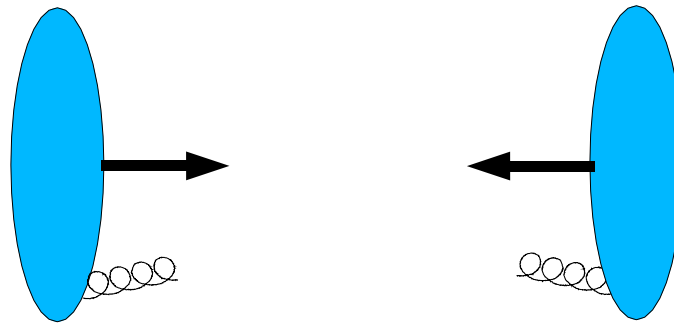
⇒ Final state: *jet quenching*.

↪ Inclusive particle production.

↪ Jet observables.

Space-time picture

Before the collision, initial state: nuclear PDF's.

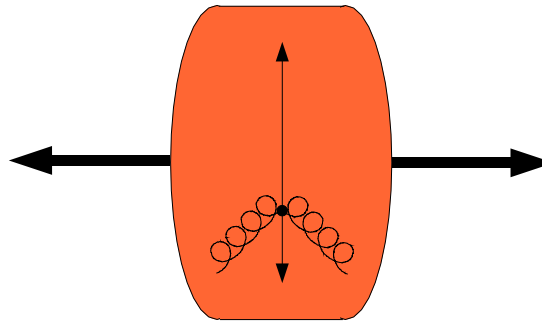


QCD factorization formula:

$$\frac{d\sigma_{AB}^h}{dp_t^2 dy} \sim \sum_{i,j} x_1 f_i^p(x_1, Q^2) \otimes x_2 f_j^p(x_2, Q^2) \otimes \frac{d\sigma^{ij \rightarrow k}}{d\hat{t}} \otimes D_{k \rightarrow h}^{\text{med}}(z, \mu_F^2)$$

Space-time picture

At $t \sim 0$

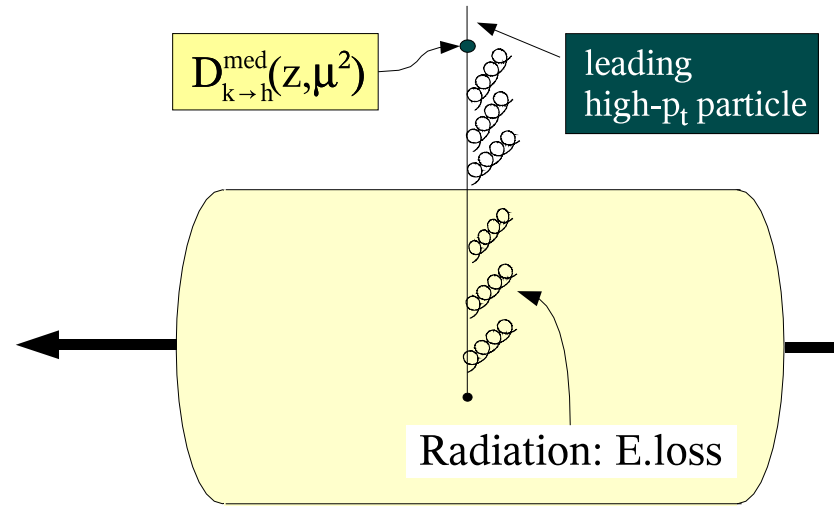


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Space-time picture

Evolution.



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Initial State

Nuclear PDF: DGLAP approaches

Nuclear modifications to PDF:

$$R_i^A(x, Q^2) \equiv \frac{f_i^A(x, Q^2)}{f_i^N(x, Q^2)}$$

Several approaches (fits, theoretical...)

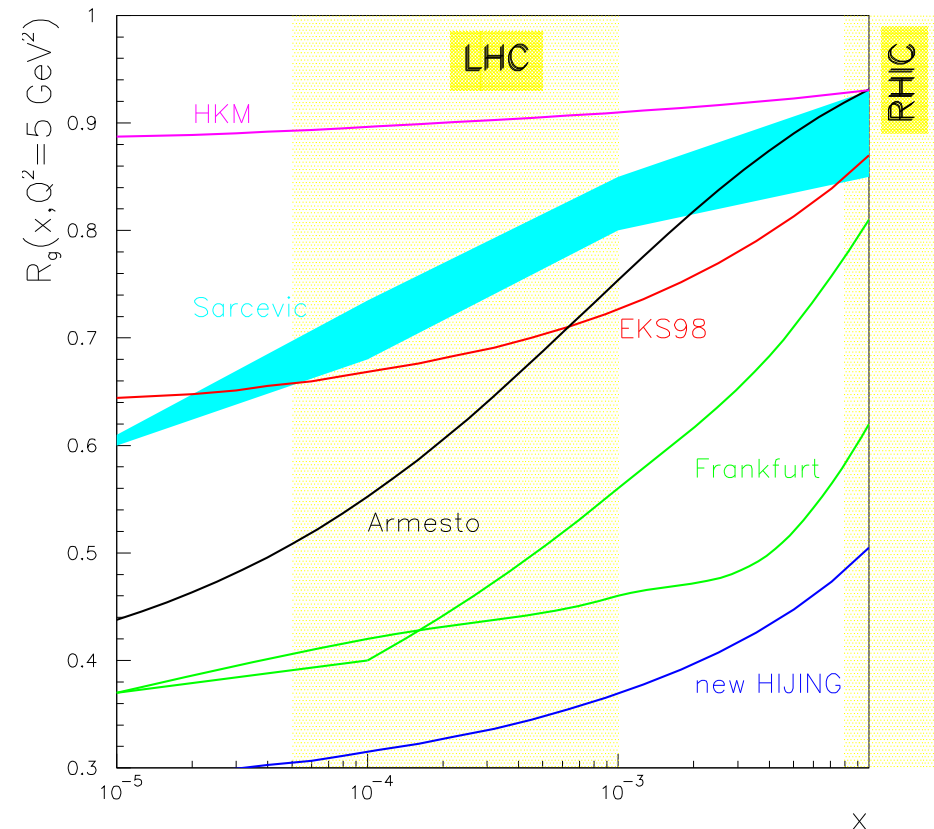
Goal of DGLAP approaches:

→ perform a set of nPDF following the procedure for protons:

⇒ Initial conditions at $Q_0 > \Lambda_{QCD}$

⇒ Evolution by DGLAP equations.

Gluons for Pb, $Q^2=5 \text{ GeV}^2$



Accardi *et al.* hep-ph/0308248

Constraints for gluons from DIS data

At small values of x , LO–DGLAP gives

$$\frac{\partial F_2^{p(n)}(x, Q^2)}{\partial \log Q^2} \propto xg(2x, Q^2).$$

This leads to

$$\frac{\partial R_{F_2}^A(x, Q^2)}{\partial \log Q^2} \propto \{R_g^A(2x, Q^2) - R_{F_2}^A(x, Q^2)\},$$

Q^2 –dependence of F_2^{Sn}/F_2^C
(NMC)

positive slope \longrightarrow

$$R_g^A(2x, Q^2) \geq R_{F_2}^A(x, Q^2).$$

(Eskola, *et al.*, PLB532, 222)

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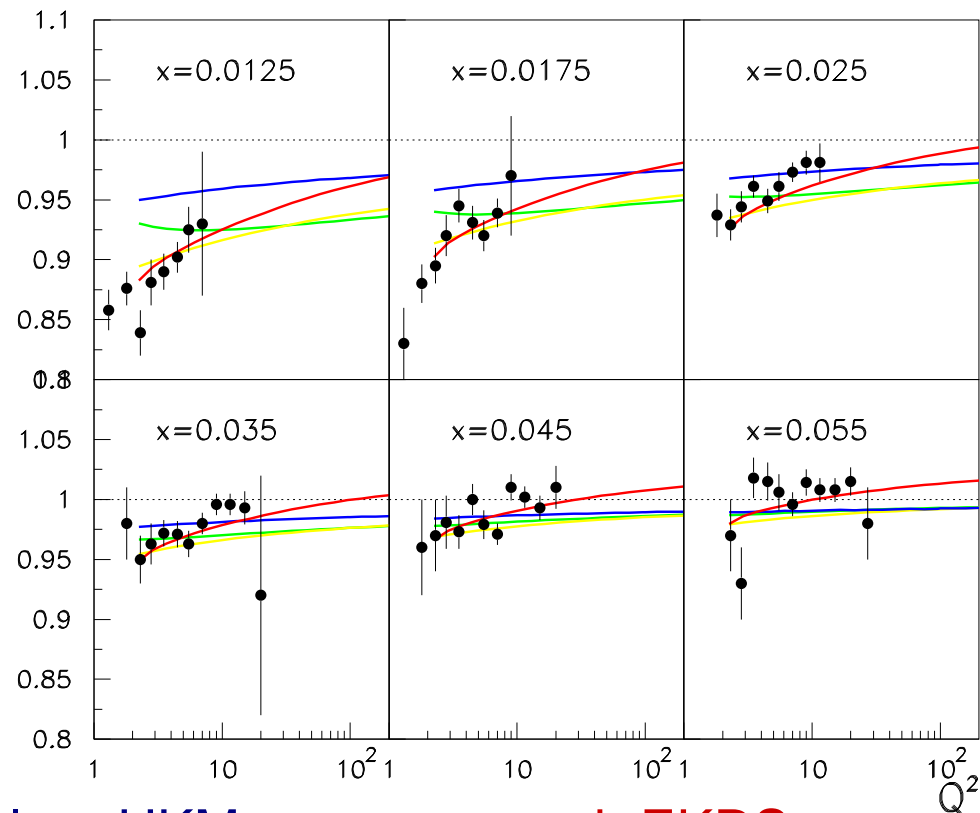
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blue: HKM

red: EKRS

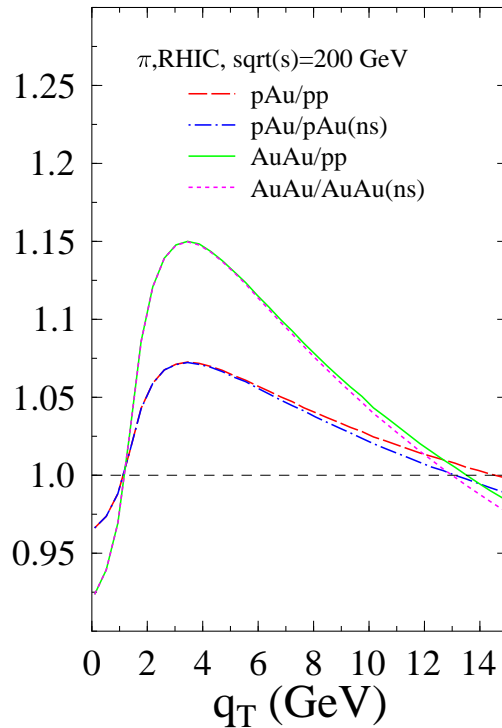
green: New HIJING

yellow: HPC

(Full DGLAP evolution)

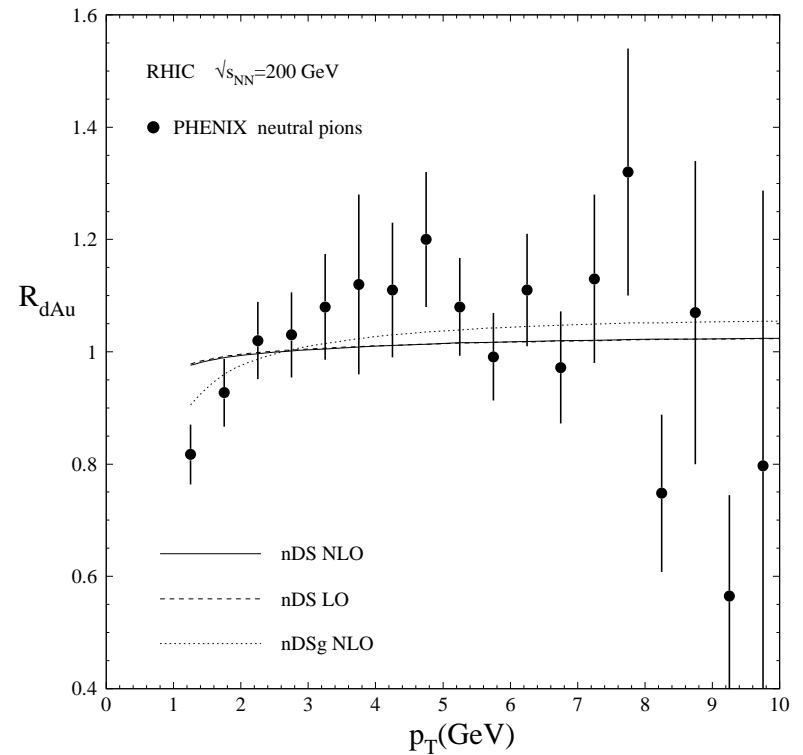
Comparison with dAu π^0 data

(PHENIX, PRL 91, 072303)



EKRS \Rightarrow small increase ($\sim 7\%$)

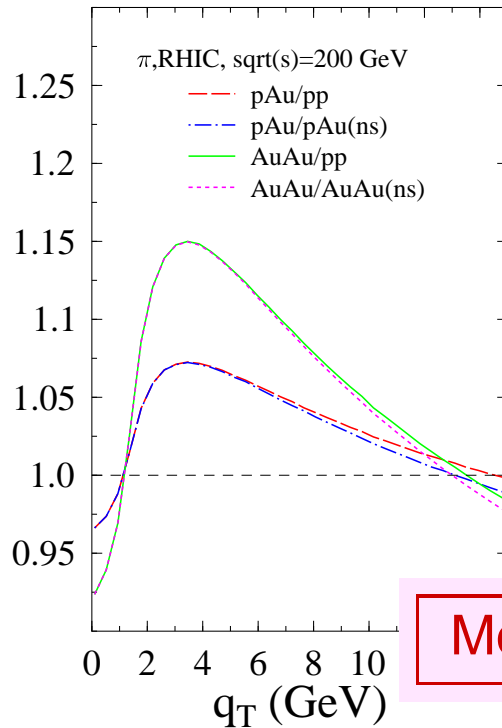
(Eskola, Honkanen NPA713 (2003) 167)



(de Florian, Sassot, hep-ph/0311227)

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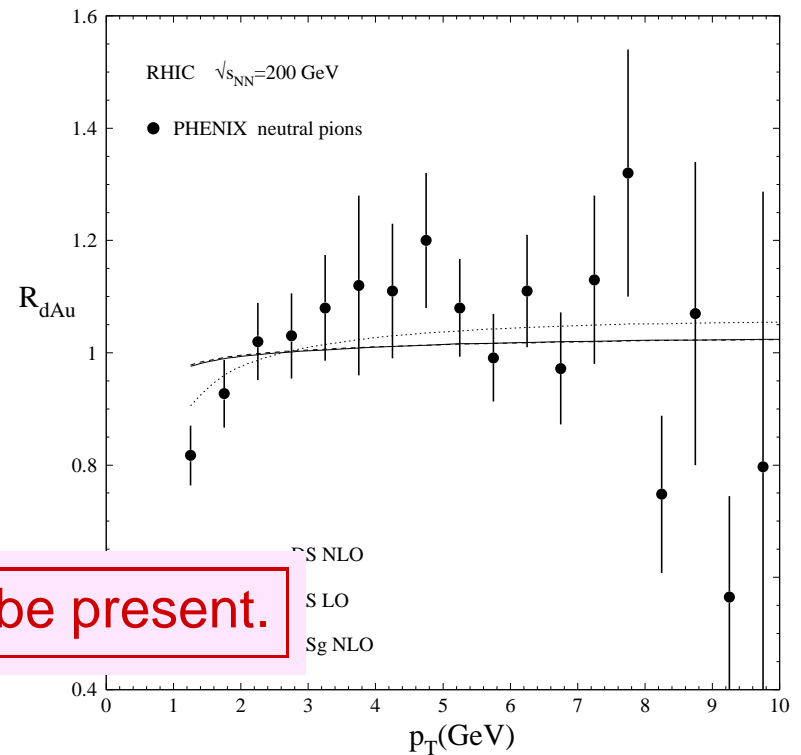
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More effects could be present.

EKRS \Rightarrow small increase ($\sim 7\%$)

(Eskola, Honkanen NPA713 (2003) 167)



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Suppression & Saturation: tomorrow's session.

- ⇒ Saturation physics proposed to explain suppression in central AuAu at $y \sim 0$
(Kharzeev, Levin, McLerran PLB561, 93)
- ⇒ dAu data \implies this is not realized at $y \sim 0$
- ⇒ However, predictions in this framework:
(Albacete, Armesto, Kovner, Salgado, Wiedemann, hep-ph/0307179;
Baier, Kovner, Wiedemann, PRD68, 054009, hep-ph/0305265 v2;
Kharzeev, Kovchegov, Tuchin PRD68, 094013 hep-ph/0307037 v2;
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- ↪ Cronin effect (enhancement) included in MV model (no evolution).

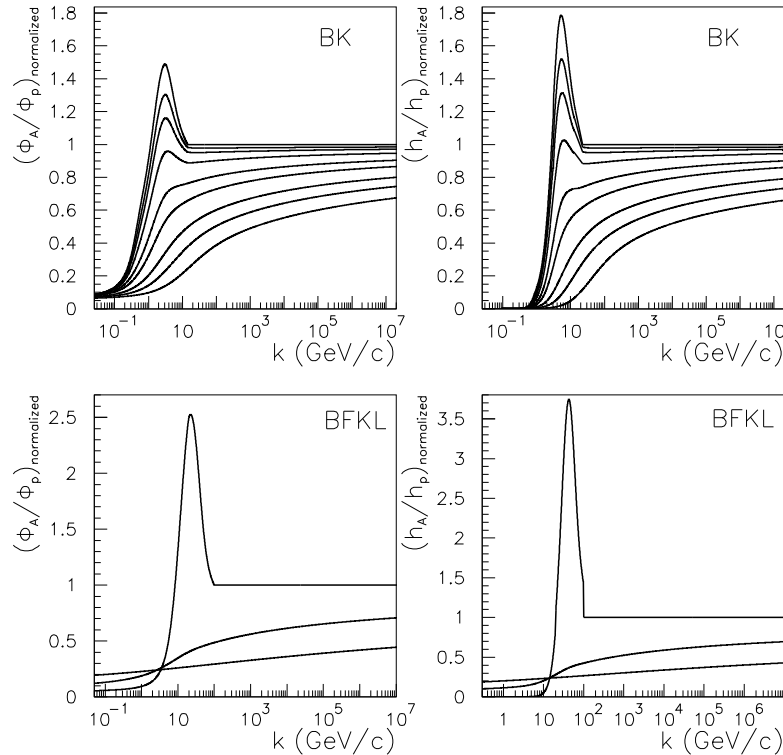
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- ↪ Cronin effect (enhancement) included in MV model (no evolution).
- ↪ Small- x evolution (BFKL, BK) suppresses the gluon densities for all p_t very efficiently.

BK and BFKL evolution erases Cronin enhancement

(Albacete, Armesto, Kovner, Salgado, Wiedemann, hep-ph/0307179)

Taken MV as initial condition for BK evolution:



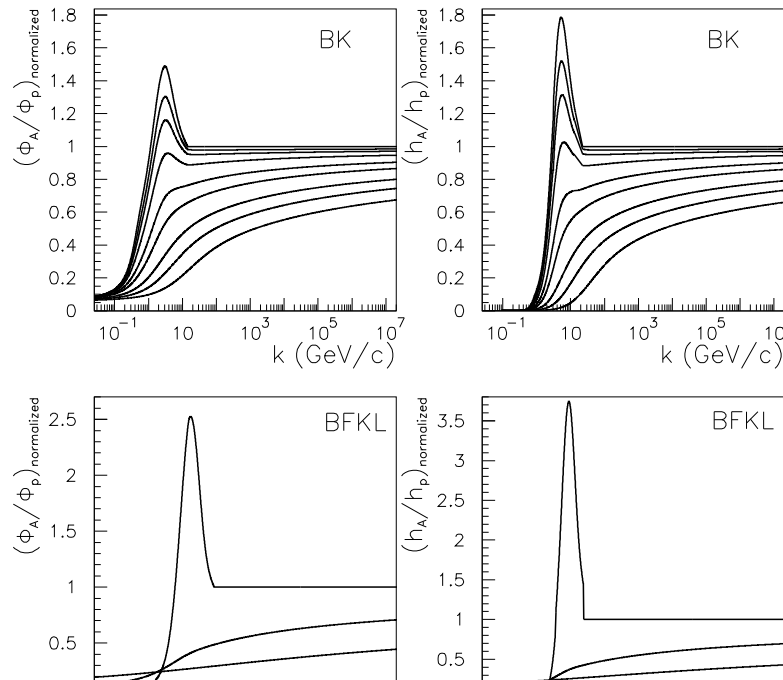
$$\Phi \rightarrow \text{MV (initial)}; h(k) = k^2 \nabla_k^2 \Phi(k)$$

$$\frac{\alpha_s N_c}{\pi} Y = 0, 0.05, 0.1, 0.2, 0.4, 0.6, 1, 1.4 \text{ and } 2$$

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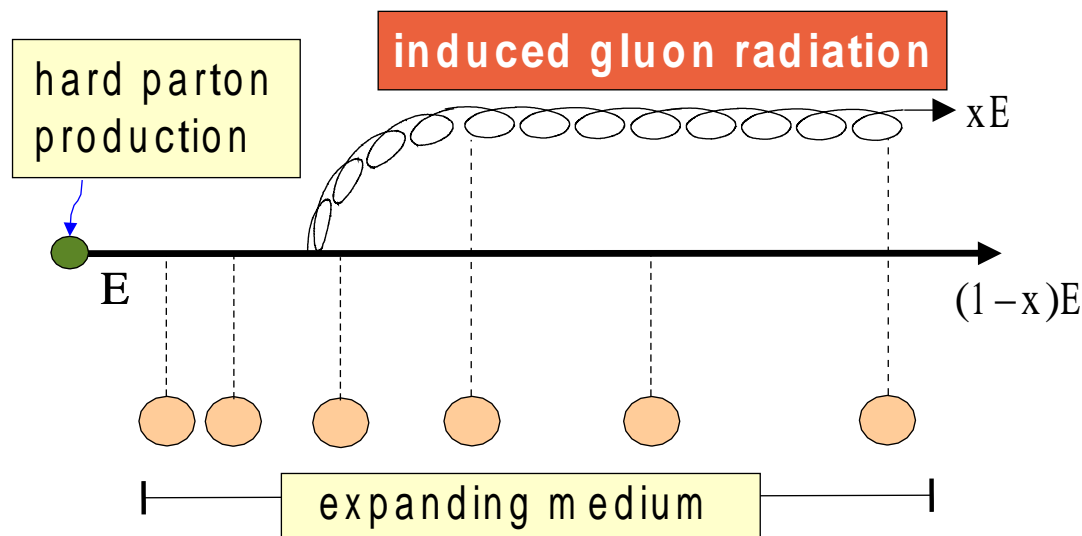
Suppression at forward rapidities → BRAHMS???

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Final State

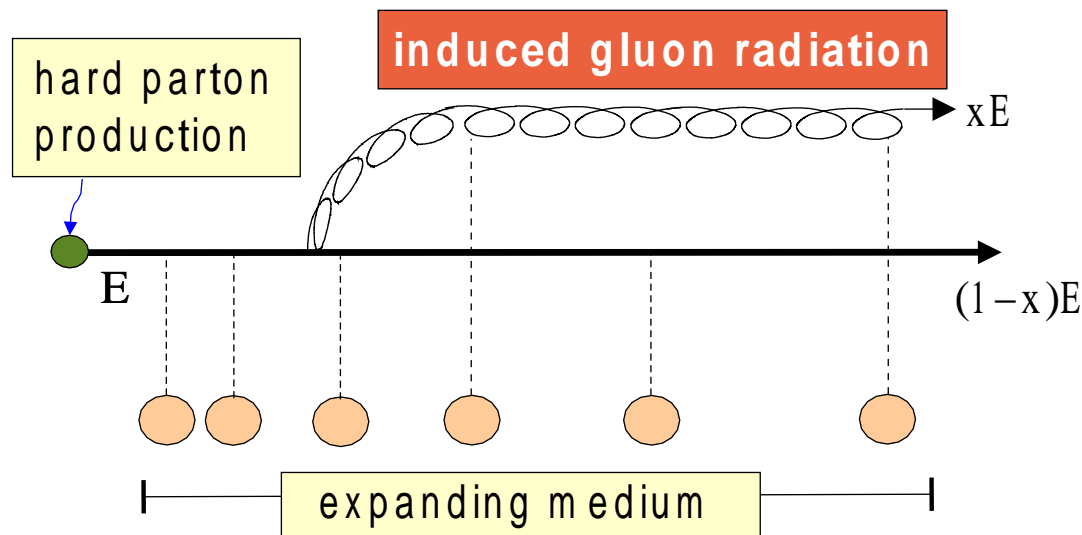
Medium-induced gluon radiation.



For media of finite length

$$\omega \frac{dI^{tot}}{d\omega dk_{\perp}^2} = \left| \int_0^L \left[\text{diagram of gluon emission from a medium element} \right] dx \right|^2 + 2\text{Re} \left(\int_0^L \left[\text{diagram of gluon emission from a medium element} \right] dx \right) \left(\int_0^L \left[\text{diagram of gluon emission from a medium element} \right] dx \right)^* + \left| \int_0^L \left[\text{diagram of gluon emission from a medium element} \right] dx \right|^2$$

Medium-induced gluon radiation.



For media of finite length

$$\omega \frac{dI^{tot}}{d\omega dk_{\perp}^2} = \left| \begin{array}{c} \text{diagram of gluon emission in medium} \\ 0 \quad L \end{array} \right|^2 + 2\text{Re} \left(\begin{array}{c} \text{diagram of gluon emission in medium} \\ 0 \quad L \end{array} \right) \left(\begin{array}{c} \text{diagram of gluon emission in vacuum} \end{array} \right)^* + \left| \begin{array}{c} \text{diagram of gluon emission in vacuum} \end{array} \right|^2$$

The medium induced gluon radiation

$$\omega \frac{dI}{d\omega dk_{\perp}^2} = \omega \frac{dI^{tot}}{d\omega dk_{\perp}^2} - \omega \frac{dI^{vac}}{d\omega dk_{\perp}^2}$$

Medium: L (length) and \hat{q} (transport coefficient).

Coherent radiation

Coherence effects are important in high energy multiple scattering processes. For a gluon emitted with energy ω and k_\perp ,

$$\varphi = \left\langle \frac{k_\perp^2}{2\omega} \Delta z \right\rangle \Rightarrow l_{coh} \sim \frac{\omega}{k_\perp^2}$$

Medium \longrightarrow transport coefficient $\hat{q} \simeq \frac{\mu^2}{\lambda}$, transverse momentum μ^2 per mean free path λ . So,

$$k_\perp^2 \sim \frac{l_{coh}}{\lambda} \mu^2 \Rightarrow k_\perp^2 \sim \hat{q} L \quad (\text{for } l_{coh} = L)$$

Let us define $\kappa^2 \equiv \frac{k_\perp^2}{\hat{q}L}$, $\omega_c = \frac{1}{2} \hat{q} L^2$

So, the phase for $\Delta z = L \longrightarrow \varphi \sim \kappa^2 \frac{\omega_c}{\omega}$

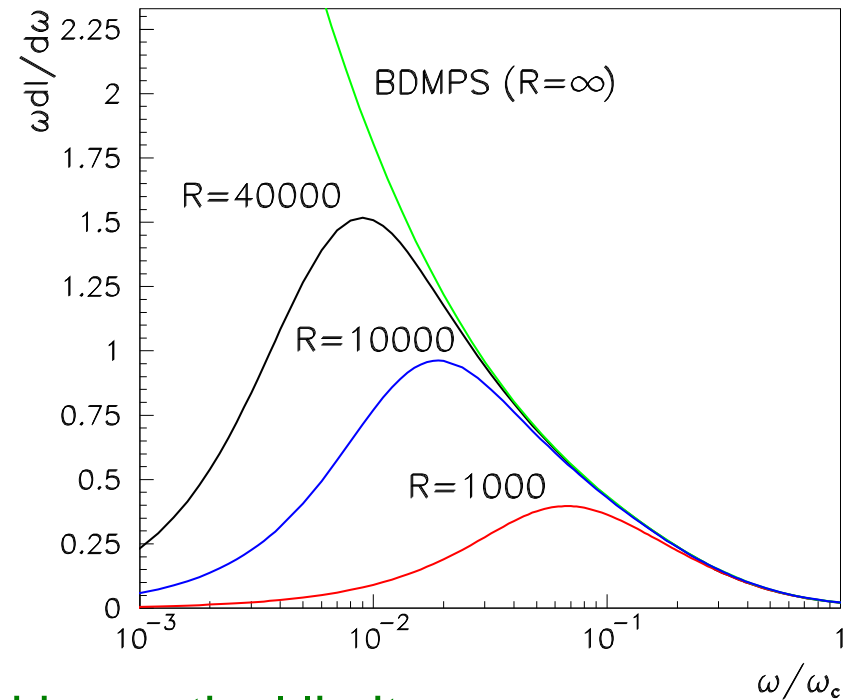
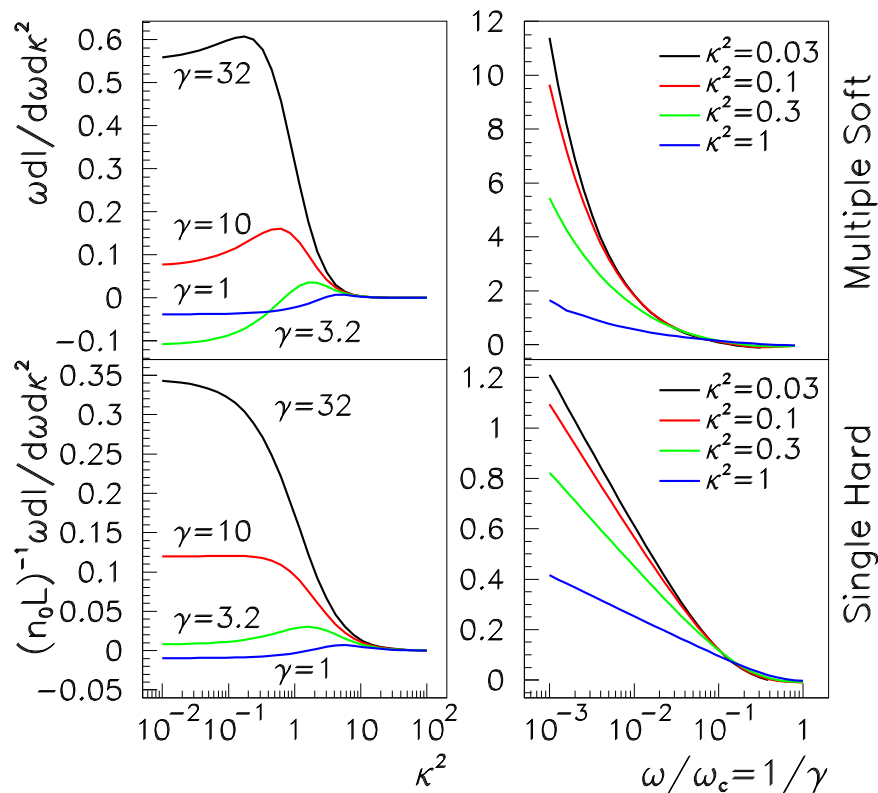
gluon emitted when $\varphi \gtrsim 1 \iff$ radiation suppressed for $\kappa^2 \lesssim \omega/\omega_c$

In cold nuclear matter: $Q_{sat}^2 = \hat{q}L \Rightarrow \kappa^2 = \frac{k_\perp^2}{Q_{sat}^2}$

Gluon energy distributions for quark jets

$$\kappa^2 = \frac{k_\perp^2}{\hat{q}L}, \quad \omega_c = \frac{1}{2}\hat{q}L^2$$

$$\omega \frac{dI}{d\omega} = \int_0^\omega dk_\perp \omega \frac{dI}{d\omega dk_\perp}$$



kinematical limit

$k_\perp \leq \omega \implies R = \omega_c L$ finite

Infrared safe.

Plateau at small $\kappa \longleftrightarrow$ coherence
gluons \implies factor N_c/C_F larger

Applications: medium-modified FF.

Model:(Wang, Huang, Sarcevic, PRL 77 2537)

$$D_{h/q}^{(\text{med})}(z, Q^2) = \int_0^1 d\epsilon P_E(\epsilon) \frac{1}{1-\epsilon} D_{h/q}\left(\frac{z}{1-\epsilon}, Q^2\right).$$

$P(\epsilon)$ probability that the hard parton loses a fraction of energy ϵ .

Independent gluon emission approx.: (BDMS, JHEP 0109:033)

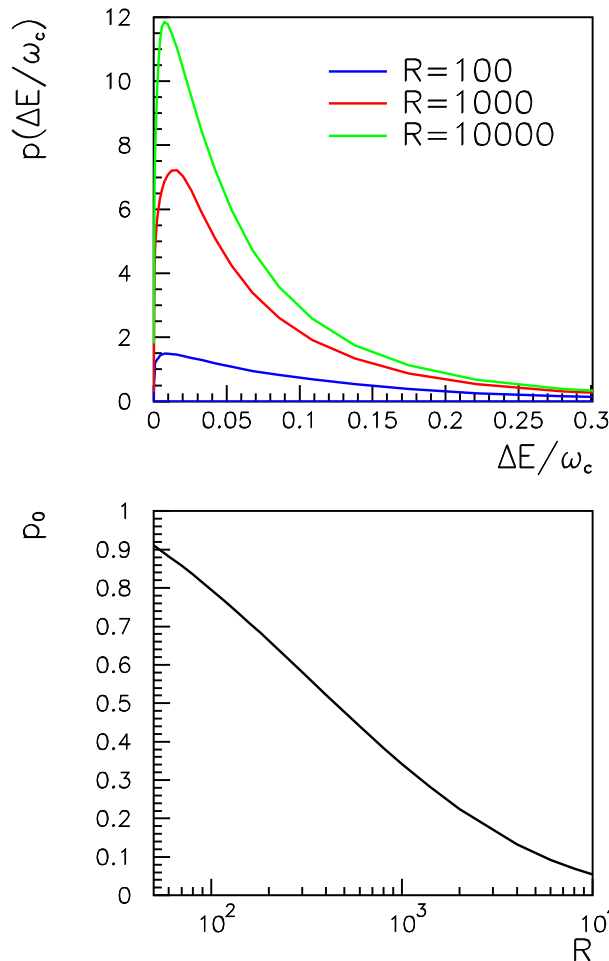
$$P_E(\epsilon) = \sum_{n=0}^{\infty} \frac{1}{n!} \left[\prod_{i=1}^n \int d\omega_i \frac{dI(\omega_i)}{d\omega} \right] \delta \left(\epsilon - \sum_{i=1}^n \frac{\omega_i}{E} \right) \exp \left[- \int d\omega \frac{dI}{d\omega} \right].$$

$$P(\epsilon) = p_0 \delta(\epsilon) + p(\epsilon)$$

$p_0 \Rightarrow$ no E.loss and $p(\epsilon) \Rightarrow$ sum for $n \geq 1$.

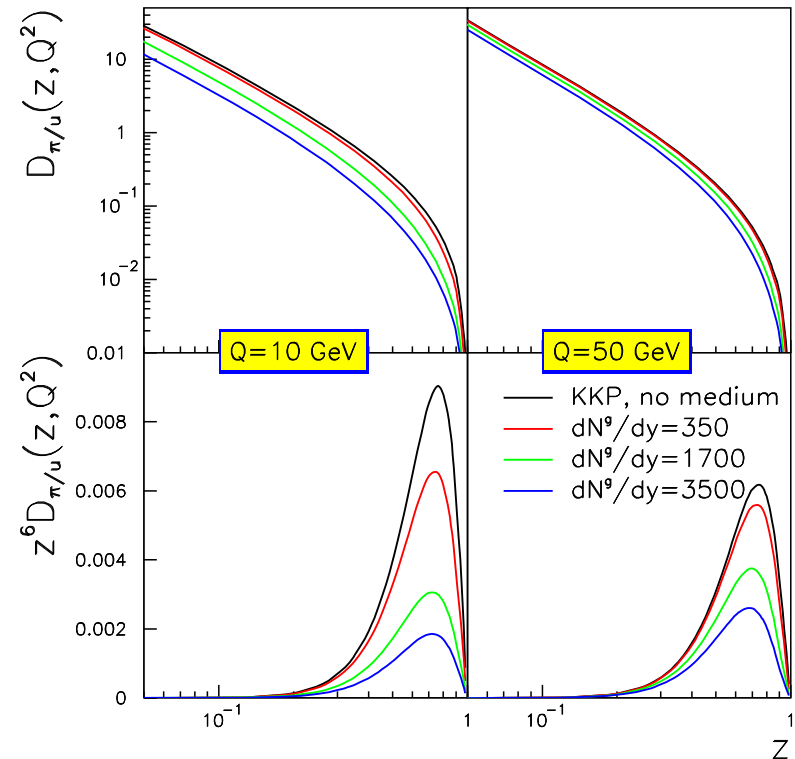
Applications: medium-modified FF.

Quenching weights for quarks.



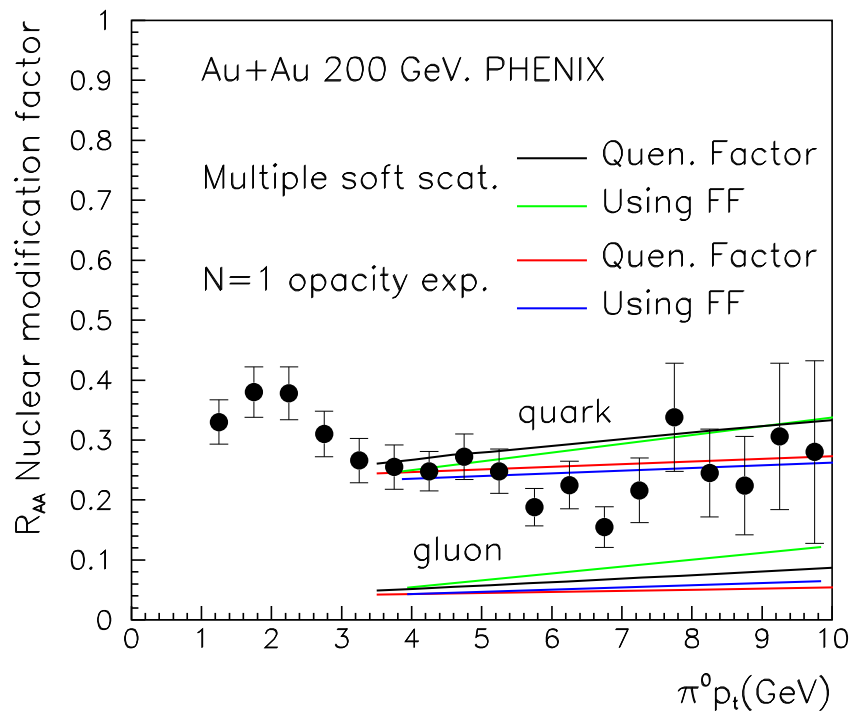
Tabulated: <http://home.cern.ch/csalgado>

$$R = \frac{\bar{\hat{q}}}{2} L^3 = \frac{L^2}{R_A^2} \frac{dN^g}{dy}$$



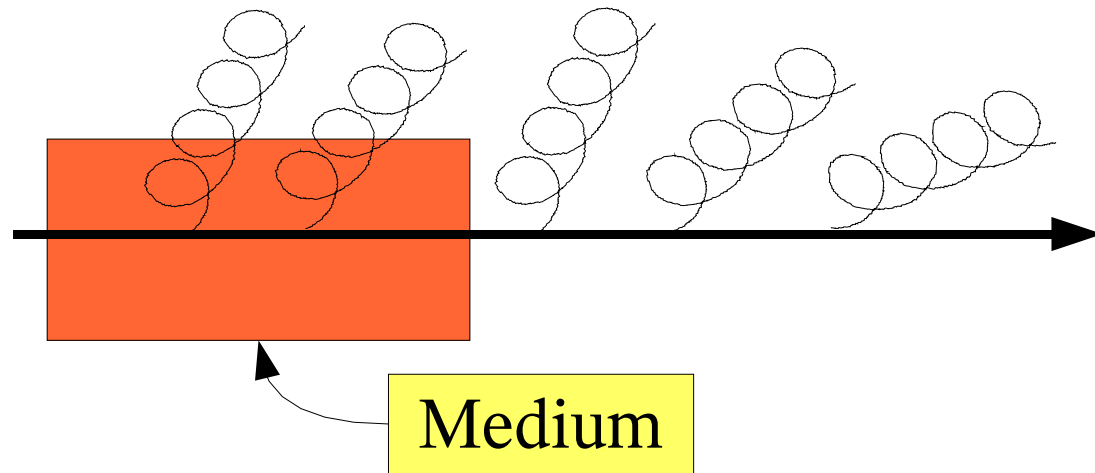
Suppression of ~ 5 for $p_t \sim 5 \div 7$ GeV $\Rightarrow R \sim 2000$.

Applications: Comparison with PHENIX data.

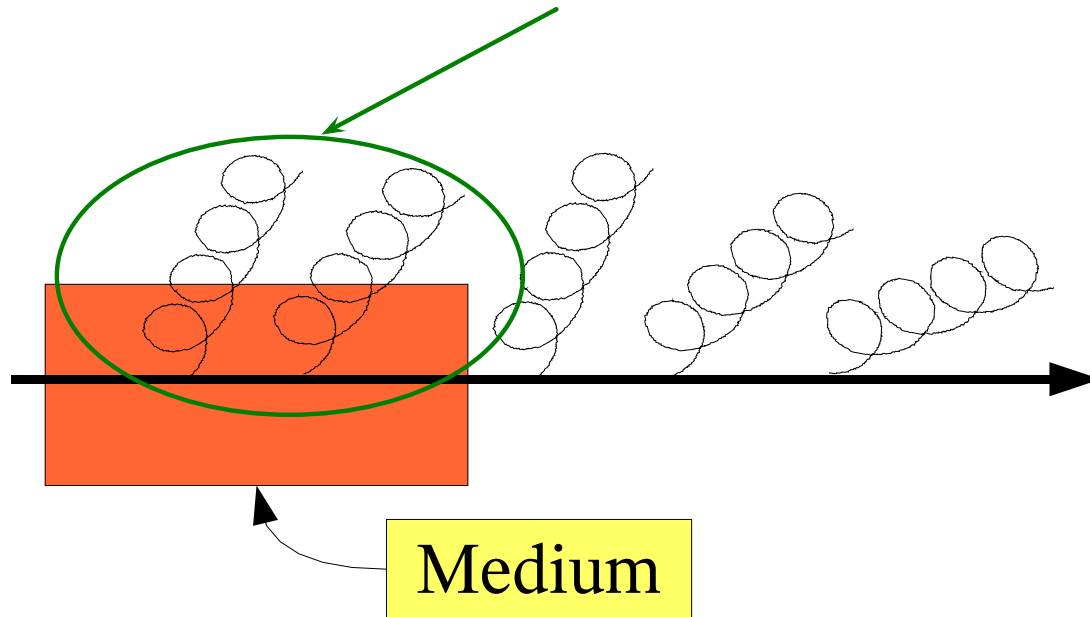


- ⇒ Factor 5 suppression needs $R \sim 1000 \div 2000$. But small- p_t region not well reproduced: additional effects? (shadowing, Cronin ...) Gyulassy, Levai, Vitev, Wang, Arleo ...
- ⇒ Smallest values of p_t are in the limit of applicability of the calculations.
- ⇒ Slope and magnitude of the effect are ok.

Jets



Can we measure this??



Jet shapes

$\rho(R)$, fraction of the jet energy inside a cone $R = \sqrt{\Delta\eta^2 + \Delta\phi^2}$

$$\rho_{\text{vac}}(R) = \frac{1}{N_{\text{jets}}} \sum_{\text{jets}} \frac{E_t(R)}{E_t(R=1)}$$

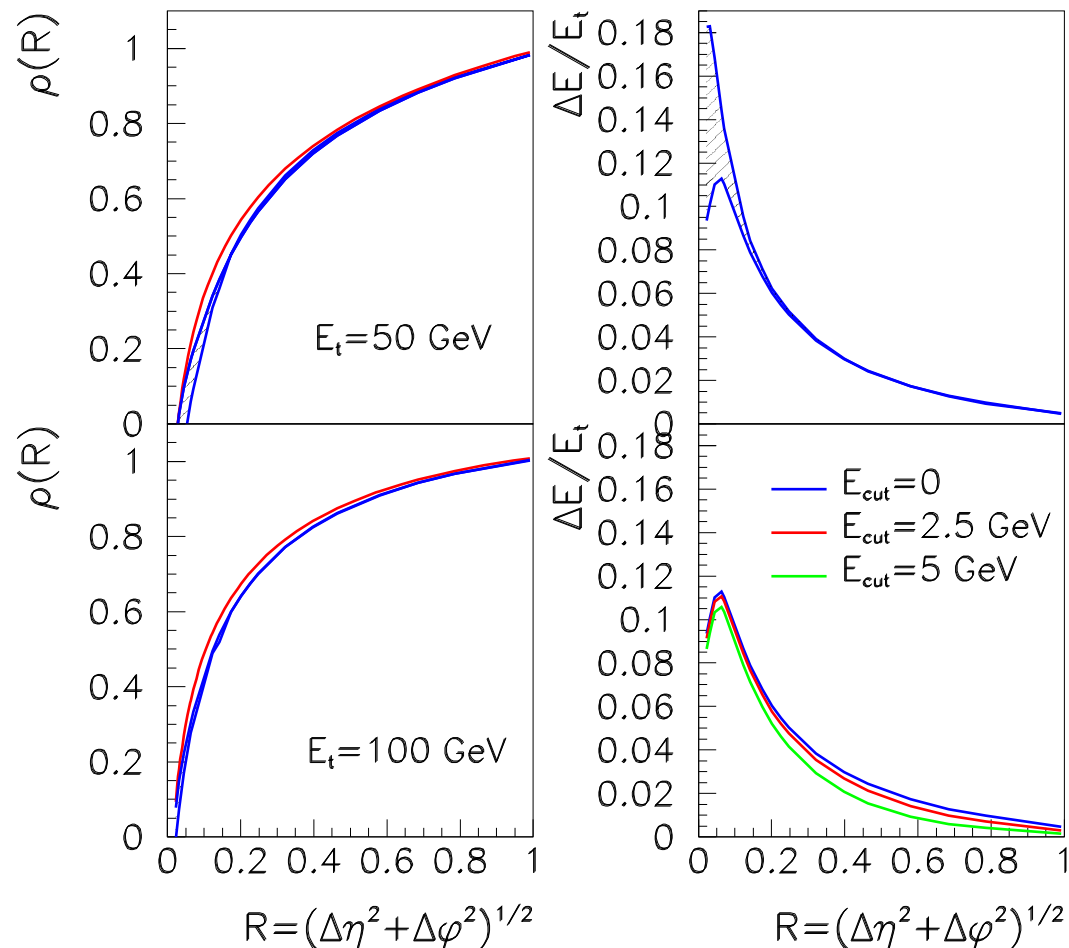
$$\rho_{\text{med}} = \rho_{\text{vac}} - \frac{\Delta E_t(R)}{E_t(R=1)}$$

Small modification \rightarrow can jet energy be determined experimentally above background??

Scaling with number of collisions for large cone angle.

Small sensitivity to IR cuts!

(Salgado, Wiedemann hep-ph/0310079)



Vacuum D0 data: Fermilab-PUB-97/242-E

Jet shapes

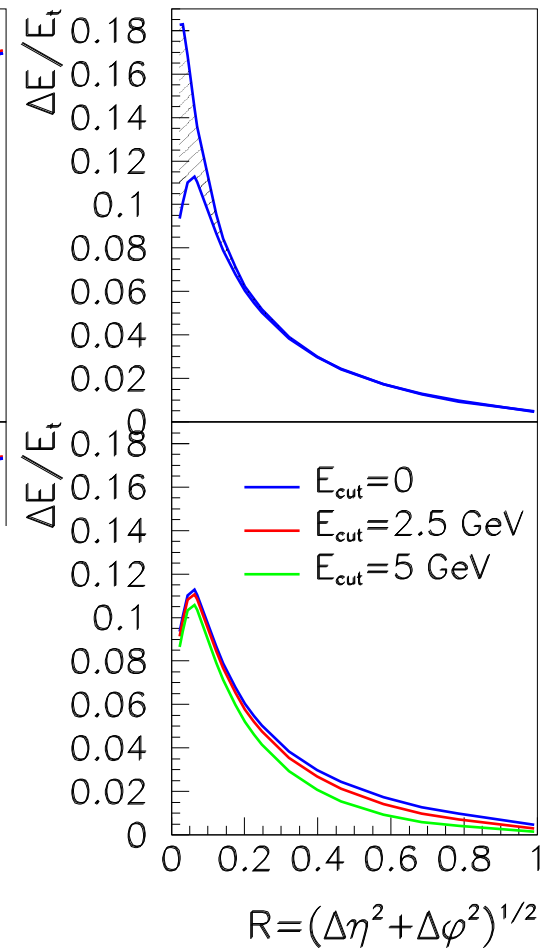
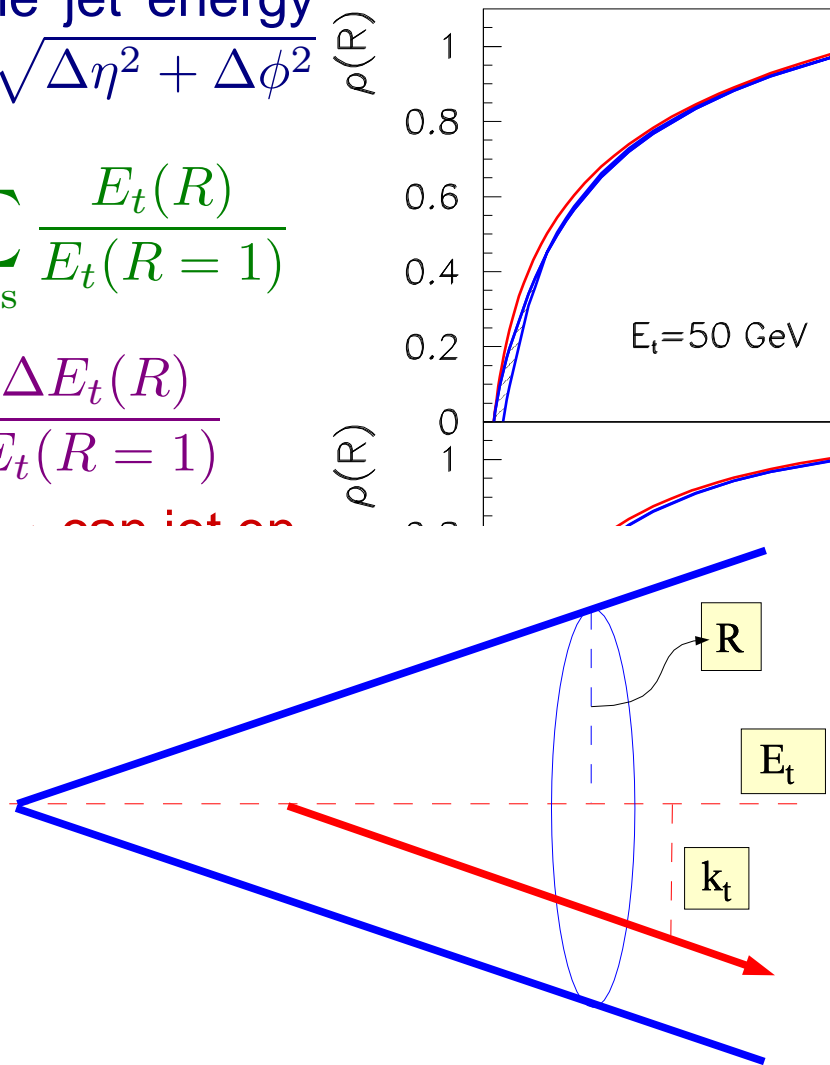
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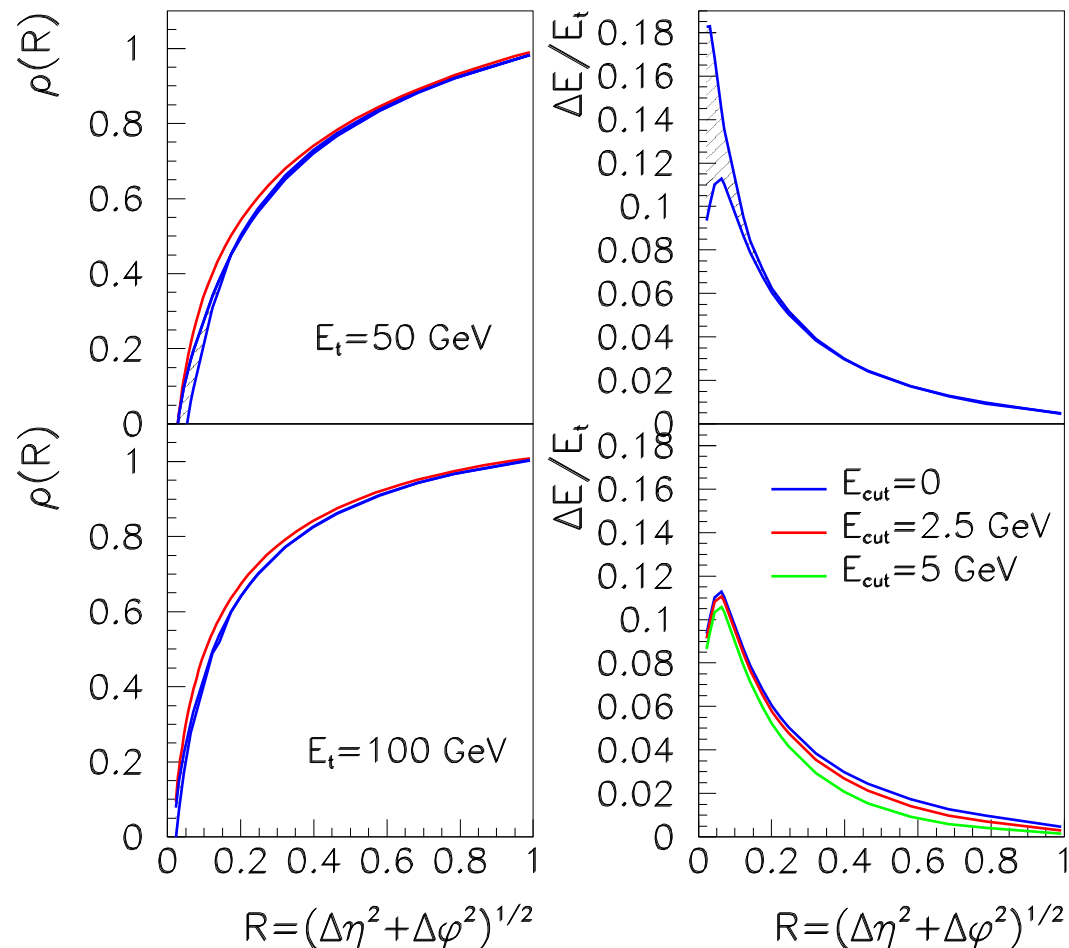
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Gluon multiplicity inside the jet.

The characteristic angular distribution of the medium-induced gluon radiation could be better observed in the quantity

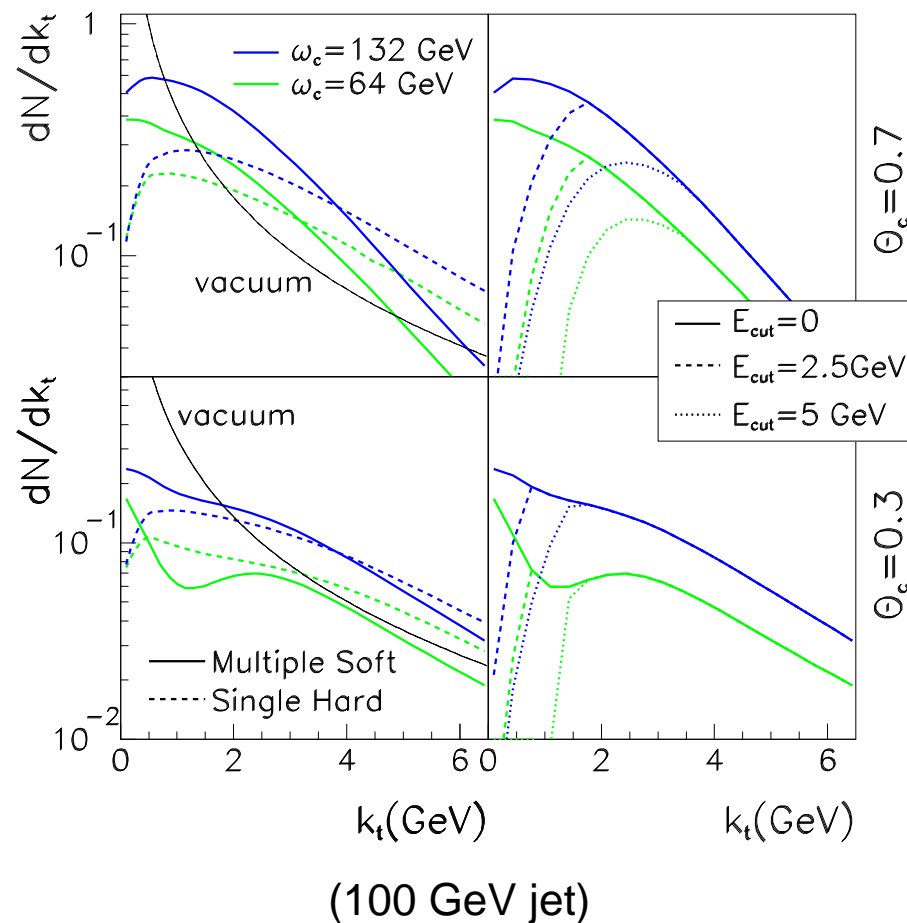
$$\frac{dN^{\text{jet}}}{dk_{\perp}} = \int_{k_{\perp}/\sin\theta_c}^E d\omega \frac{dI}{d\omega dk_{\perp}}$$

For the vacuum we simply use

$$\frac{dI_{\text{vac}}}{d\omega dk_{\perp}} \sim \frac{1}{\omega} \frac{1}{k_{\perp}}$$

Needs a more quantitative analysis.

But, effect based mainly on kinematics!



Conclusion

- ⇒ High-pt particle production is affected by the medium → good probe to study its properties.
- ⇒ RHIC high- p_t results strongly point to a final state effect in central AuAu.
 - ↪ In agreement with jet-quenching interpretation.
 - ↪ dAu data essential.
- ⇒ DGLAP+NMC ⇒ not very strong gluon shadowing for $x \gtrsim 0.01$.
- ⇒ Small- x evolution removes Cronin very fast ⇒ forward rapidities (?)
- ⇒ Medium-induced gluon radiation computed for realistic length & kinematics: We recover BDMPS for $R \rightarrow \infty$. Small IR-sensitivity.
- ⇒ Angular dependence of the radiation → study Jets.
- ⇒ Jet shapes → Can these effects be seen @ RHIC?
 - ↪ Small effect in the azimuthal redistribution of jet energy.
 - ↪ Gluon multiplicities inside the jets could be a clean observable.

DGLAP analyses

Comparison EKS, HKM, nDS (de Florian and Sassot, hep-ph/0311227)

